$\square$

Congratulations to the Winners of the Hog Strategy Contest
1st Place with 146 wins:
"A submission scores a match point
A five-way tie for first place! each time it has an expected win rate strictly above 50.0001\%."


Congratulations to Timothy Guo, Shomini Sen, Samuet Berkun, Mitchell Zhen, Lucas Clark, Dominic de Bettencourt, Allen Gu, Alec Li, Aaron Janse
hog-contest.cs61a.org
Box-and-Pointer Notation

The Closure Property of Data Types

## Box-and-Pointer Notation in Environment Diagrams

Lists are represented as a row of index-labeled adjacent boxes, one per element Each box either contains a primitive value or points to a compound value

$$
\underset{\text { pair }}{\text { Global frame }} \longrightarrow \begin{gathered}
\text { list } \\
0
\end{gathered} \underbrace{1}_{1} \begin{aligned}
& 1 \\
& \hline
\end{aligned}
$$

pair $=[1,2]$
Lists can contain lists as elements (in addition to anything else)

Box-and-Pointer Notation in Environment Diagrams

Lists are represented as a row of index-labeled adjacent boxes, one per element Each box either contains a primitive value or points to a compound value

```
pair = [1, 2]
    2
3 nested_list = [[1, 2], [],
    [[3, False, None],
    [[3, False, None],
    [4, lambda: 5]]]
```

    [4, lambda: 5]]]
    ```
\begin{tabular}{|c|}
\hline Slicing \\
\\
(Demo) \\
\\
\hline
\end{tabular}

Slicing Creates New Values
```

1 digits = [1, 8, 2, 8]
2 start = digits[:1]
3 middle = digits[1:3]
4 end = digits[2:]
-5 full = digits[:]

```


Processing Container Values

\(\square\)

\section*{Implementing the Tree Abstraction}
```

    def tree(label, branches=[]):
    ```
    return [label] + branches
    def label(tree):
    return tree[0]
def branches(tree): return tree[1:]


A tree has a root label and a list of branches Each branch is a tree
A tree with zero branches is called a leaf A tree starts at the root Each location in a tree is called a nod Each node has a label that can be any value One node can be the parent/child of another The top node is the root node
People often refer to labels by their locations: "each parent is the sum of its children"
Tree Abstraction


Peple often refer to labels by their locations "each parent is the sur of children"

\(\square\)
\begin{tabular}{|c|}
\hline Tree Processing Uses Recursion \\
\hline Processing a leaf is often the base case of a tree processing function \\
\hline The recursive case typically makes a recursive call on each branch, then aggregates \\
\hline def count_leaves(t) : \\
\hline \multirow[t]{2}{*}{if is_leaf( t ):} \\
\hline \\
\hline else: \\
\hline \multirow[t]{2}{*}{branch_counts = [count_leaves(b) for b in branches(t)] return sum(branch_counts)} \\
\hline \\
\hline (Demo) \\
\hline
\end{tabular}

\section*{Discussion Question}

Implement leaves, which returns a list of the leaf labels of a tree
Hint: If you sum a list of lists, you get a list containing the elements of those lists
\(\ggg \operatorname{sum}([[1],[2,3],[4]],[])\) def leaves(tree) :
\([1,2,3,4]\)
\(\ggg>\operatorname{sum}([1]],[])\)

\([1]\) \(\begin{array}{ll}\ggg \operatorname{sum}([[1]],[]) & \ggg \\ {[1]} \\ \ggg \operatorname{leaves}(f i b \\ \operatorname{sum}([[[1]],[2]],[]) & {[1,0,1,0,1,1,0,1]}\end{array}\) \(\rightarrow>\operatorname{sum}([[[1]],[2]],[]) \quad[1,0,1,0,1,1,0,1]\) return [label(tree)] else:
return sum(List of leaf labels for each branch, [])

\section*{branches(tree)}
leaves(tree)
[branches(b) for b in branches(tree)]
[leaves(b) for b in branches(tree)]
[s for \(s\) in leaves(tree)]
[s for \(s\) in
[branches(s) for \(s\) in leaves(tree)]
[leaves(s) for \(s\) in leaves(tree)]

\section*{Creating Trees}

A function that creates a tree from another tree is typically also recursive
```

def increment_leaves(t):
""Return a tree like t but with leaf labels incremented."""
if is_leaf(t):
return tree(label(t) + 1)
else:
bs = [increment_leaves(b) for b in branches(t)]
return tree(label(t), bs)
def increment(t):
'""Return a tree like t but with all labels incremented."""
return tree(label(t) + 1, [increment(b) for b in branches(t)])

```

\section*{Example: Summing Paths}```

